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Integrating Machine Learning Models to Building Codes and Standards: Establishing Equivalence through Engineering Intuition and Causal Logic

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Abstract

The traditional approach to formulating building codes is often slow, labor-intensive, and may struggle to keep pace with the rapid evolution of technology and domain findings. Overcoming such challenges necessitates a methodology that streamlines the modernization of codal provisions. This paper proposes a machine learning (ML) approach to append a variety of codal provisions, including those of empirical, statistical, and theoretical nature. In this approach, a codal provision (i.e., equation) is analyzed to trace its properties (e.g., engineering intuition and causal logic). Then a ML model is tailored to preserve the same properties and satisfy a collection of similarity and performance measures until declared equivalent to the provision at hand. The resulting ML model harnesses the predictive capabilities of ML while arriving at predictions similar to the codal provision used to train the ML model, and hence, it becomes possible to adopt in line with the codal expression. This approach has been successfully examined on seven structural engineering phenomena contained within various building codes, including those in North America and Australia. Our findings suggest that the proposed approach could lay the groundwork for implementing ML in the development of future building codes.

Keywords: Building codes; Machine learning; Prediction.

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23 **1.0 Introduction**

24 Building codes are guiding documents that home rules and recommendations aimed to standardize
25 civil engineering guidelines and processes pertaining to design, analysis, construction, etc. (ASCE
26 2016). Such codes remain the cornerstone of civil engineering, providing a framework to establish
27 building occupants' safety, health, and general welfare.

28 The process of creating codal provisions begins with collecting and analyzing data, often gathered
29 from past building failures, tests, simulations, and empirical/practical experiences gained from
30 well-documented incidents. All such data is systematically archived, studied, and evaluated to
31 understand and learn from it to avoid repeating past failures (Ellingwood 1994). The same is then
32 formulated and incorporated into the building codes. For instance, the International Building Code
33 (IBC) (IBC 2018) stipulates the minimum standards for various aspects, like structural integrity
34 and fire safety. By complying with such codes, engineers can minimize the risk of building
35 collapse, fire hazards, and other potential accidents. Thus, adherence to codal provisions is not
36 merely voluntary but a legal obligation and ethical responsibility (Law 2021). The open literature
37 shows various cases where non-compliance with building codes resulted in catastrophic loss of
38 life and property (Windapo and Cattell 2010; Yakubu 2019).

39 Many codal guidelines are communicated via equations (formulas). These formulas display the
40 key parameters and the relationship of how such parameters are tied to a specific phenomenon.
41 For example, Eq. 1 shows that the moment capacity of compact W-shaped steel beams is a function
42 of the plastic section modulus, Z , and the yield strength (f_y) of the structural steel. In this format,
43 an engineer can simply predict and/or evaluate the expected moment capacity of a given beam via

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44 Eq. 1. More importantly, an engineer may also causally infer that an increase in either (or both)
45 parameters can increase the moment capacity of the beam (and vice versa).

$$46 \quad M = f_y \times Z \quad (1)$$

47 While some formulas stem from the deterministic nature rooted in physics and engineering
48 principles, others are probabilistic, empirical, or arrived at via statistical methods (Lie 1992;
49 Marasco et al. 2021). Despite the origin of codal provisions, variants of such provisions exist in
50 building codes. Building committees have been noted to accept such variants as without these
51 committees, provisions would not have been accepted and included in building codes.

52 In recent years, machine learning (ML) has shown great success in many fields, including civil
53 engineering. ML models can analyze vast datasets, identify complex patterns, and make accurate
54 predictions. A look into the existing literature displays studies wherein predictions from ML are
55 reported to exceed those obtained from national and international building codes (Aladsani et al.
56 2022; Cakiroglu et al. 2022; Degtyarev and Tsavdaridis 2022; Naser 2023b; Tarawneh et al. 2021;
57 Yahiaoui et al. 2023). This begs the question of how we can leverage such models.

58 However, ML models differ significantly from codal provisions. At the moment, most ML models
59 remain driven by the supplied data. For instance, where a building code might specify an equation
60 to calculate wind loads based on the height and location of a building, a ML model would first be
61 trained to use a database of historical wind data and building performance to predict the same
62 phenomenon easily. While ML models may excel at making predictions based on the patterns in
63 the training data that may indeed surpass predictions obtained from codal provisions, the same

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64 models can struggle when confronted with scenarios or data that significantly deviate from their
65 training set (Krueger et al. 2021).

66 Furthermore, the dynamic nature of ML models, which are often updated and changed as they
67 learn from new data, contrasts sharply with the static nature of building codes (which are updated
68 but at a much more infrequent rate). For instance, the specifics of the ML model (algorithmic
69 architecture, hyperparameters, etc.) used to predict a specific phenomenon may change
70 significantly over time as the model is fed with new data. This may present a potential issue for
71 engineers who rely on consistency in their design processes (Paleyes et al. 2022).

72 Perhaps, most importantly, is this lack of transparency of some ML models. This opaqueness can
73 pose difficulties when attempting to integrate ML models into building codes, as these codes need
74 to have clearly defined and understandable criteria so that engineers can follow and verify
75 compliance (Naser and Ross 2022). While the data-driven nature of ML is its strength, it is
76 fundamentally elemental not to overlook the value of engineering principles, intuition, and domain
77 knowledge – especially in our field where decisions can impact occupants’ safety (Naser 2021b).

78 Understandably, engineers may remain skeptical of ML models due to the above challenges and
79 the absence of a regulatory framework that allows such models to be included in building codes.
80 This absence of a framework means there are no defined standards to follow. This lack of standards
81 makes it difficult for engineers to fully trust and adopt ML models. For example, engineers might
82 be wary of using an ML model if there is not a universally accepted standard for such ML models.
83 Given the absence of a structured way to integrate ML models into the design and construction

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84 processes outlined by the building codes, engineers often opt for traditional, code-approved
85 methods – even in scenarios requiring performance-based principles or out-of-the-box solutions.

86 On a more positive note, the rapid advancements in ML have now allowed the integration of
87 eXplainable AI (XAI), both of which can help create more reliable and interpretable models that
88 could be adopted into building codes. These two concepts refer to methods and techniques that
89 allow users (i.e., engineers) to understand ML models' decision-making processes (Emmert-Streib
90 et al. 2020). For instance, if a ML model could explain that it predicts a specific outcome (e.g.,
91 sectional capacity) based on specific characteristics of the building design (such as material
92 properties and geometric features), engineers would be more confident in integrating these insights
93 into their work than if the ML was a traditional blackbox model. Simply, if a ML model can explain
94 its decisions in a way that aligns with the stipulations of codal provisions, this could significantly
95 enhance the potential for ML's integration into these codes.

96 Providing transparency and a deeper understanding of the underlying relationships in the data can
97 bridge the gap between the dynamic, data-driven world of ML and the static, more calm nature of
98 building codes. From this lens, this paper proposes such a methodology. In this methodology, the
99 first stage analyzes a codal equation to trace its properties (e.g., logic). Then, a ML model is
100 tailored to learn and map the same logic – thereby transforming into a higher-order model that
101 preserves the same properties of the codal equation. Finally, the ML model is tuned on big data to
102 achieve superior performance, given the ability of ML to accommodate highly nonlinear relations.
103 Our findings indicate that the proposed approach could set the stage for ML implementation in
104 future building codes. While significant research and development are needed to refine these

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105 techniques and demonstrate their reliability and effectiveness in the context of civil engineering
106 and the involvement of regulatory and code-developing organizations, this work and its findings
107 hope to jump-start a serious conversation toward such an effort.

108 **2.0 A look into codal provisions**

109 Codal provisions often undergo a series of iterations and must bypass rigorous discussions/voting
110 by regulatory bodies, committee members, and the general public. Such provisions are commonly
111 developed from first principles (i.e., mechanics). In the event that first principles are absent or
112 immature, provisions can also be derived through statistical treatment of the outcome of physical
113 tests or, to a lesser extent, numerical simulations.

114 In physical tests, a series of specimens are designed with preset features identified by various
115 means (including empirically) and tested to generate an understanding that ties the examined
116 features to the phenomenon at hand (i.e., flexural response). The outcome of such an investigation
117 is then analyzed via statistical regression. To a certain extent, civil engineers favor using linear
118 and nonlinear regression (Benjamin and Cornell 2014). Both forms of regressions home a number
119 of assumptions that need to satisfy the data at hand as well as those pertaining to pre-selected
120 parametric forms (e.g., the use of linear regression implies the validity of linear and additive nature
121 of features, etc.) some of which may or may not be satisfied.

122 Evidently, a proper statistical regression analysis reduces to finding the best coefficients that can
123 improve the accuracy of the pre-selected parametric form from the available tests/simulations data
124 (Ribarič et al. 2008). Such an expression is further treated to attain the expected reliability
125 measures inherently required by a building code's technicalities. Once such an expression is fully

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126 verified, vetted, and voted upon, this expression is likely to be incorporated into a guiding
127 document. This procedure has been duly noted in our literature, and one of the recent examples is
128 that developed by Kuchma et al. (2019), credited with updating the one-way shear design
129 provisions for reinforced concrete in the latest ACI 318 code adopted by the American Concrete
130 Institute.

131 Depending on the comprehensiveness of a testing campaign, it is quite likely that additional tests
132 or numerical simulations can be added to supplement the data at hand. For example, Franssen and
133 Dotreppe (2003) followed a similar approach when developing the basis for Eurocode 2's
134 assessment method for the fire resistance of columns. Similarly, Wade et al. (1997) combined tests
135 with numerical simulations to derive an equation to evaluate the fire resistance of reinforced
136 concrete columns for the Australian building code (AS3600). Other examples can also be found
137 elsewhere (Feldman and Bartlett 2005; Ollgaard et al. 1971).

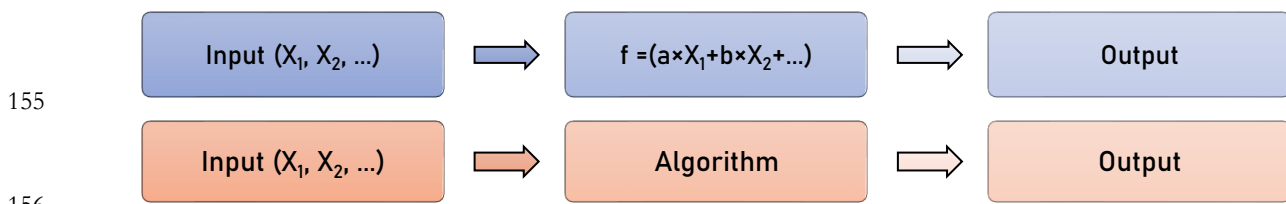
138 This work argues that, with the presence and/or absence of first principles, and when the primary
139 motivation behind utilizing statistical-based expressions in building codes is their capacity to best
140 fit existing data, then it is of merit to utilize higher-order models (such as those that fall under tree-
141 based and neural network models, etc.) also capable of best fitting the data in a more accurate
142 manner than that provided by the traditional counterparts. Noting how such models can better
143 handle high dimensional data, has non-parametric freedom, and less adherence to data-related
144 assumptions positions this method for creating suitable codal provisions.

145 A supporting philosophical view is that, for the same data and features, the statistical-based
146 procedure of iteratively fitting a codal expression by best-fitting the coefficients of its predefined

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147 form can be viewed similarly to training a ML model to learn patterns in the available data (see
148 Fig. 1). A primary difference is that the data at hand tune the coefficients for the already-defined
149 parametric form of the former and the algorithmic logic (internal model structure) for the latter.
150 One can then view the parametric form to be equivalent to the algorithmic logic since both tie the
151 key parameters into arriving at the predictions. Yet, a critical difference between the above two
152 approaches is that we are familiar with the procedure of statistical regression and, hence are able
153 to trace the steps carried out to interpret the outcome of such analysis. As will be seen in Sec. 3,
154 recent advances in explainability have now made this possible for ML (Molnar 2019).



155
156
157 Fig. 1 A simplified illustration depicting two approaches for prediction (please note that
158 additional steps could be involved (i.e., training, fitting, etc.) in a prediction problem).

159 3.0 Proposed methodology

160 3.1 General description

161 Suppose the same logic and properties of an empirical codal provision (i.e., equation) were
162 imposed on a superior high dimensional ML model. In this case, such a model can be considered
163 a natural substitute for the statistically-derived equation, as the model can now arrive at predictions
164 and interpret their outcomes similar to the codal equation.

165 This becomes of importance as, in reality, while many of the phenomena tackled by civil engineers
166 may not fully conform to the assumptions inherent in statistical methods used to derive empirical
167 expressions, engineers still apply domain knowledge to assign the position and interaction between

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168 the involved parameters fitted into such expressions. Thus, the proposed methodology starts by
169 constraining the algorithmic structure of a candidate ML model to one that imitates the same
170 characteristics (in terms of engineering logic, domain knowledge, etc.) and the essence of the codal
171 provision at hand.

172 This process is defined herein as *model equivalence*. While there could be multiple ways to
173 establish equivalence (as will be detailed in Sec. 5.0), this work establishes equivalence by
174 leveraging two eXplainable artificial intelligence methods, namely partial dependence plots (PDP)
175 and accumulated local effects (ALEs) to constrain the algorithmic structure to yield PDPs/ALEs
176 similar to those obtained from the codal equation (to a pre-specified degree). Such a degree is
177 outlined via several similarity measures, five of which will be presented below. Finally, and once
178 equivalence is established, model predictions are compared against those obtained from the codal
179 equation via statistical measures. This section starts by covering the principles of PDP/ALE and
180 then dives into the similarity measures selected to establish equivalence.

181 *3.2 Equivalence through partial dependence plots (PDP)*

182 The PDP explains ML models by depicting an individual (or more) feature's *marginal effect* on
183 the prediction of a ML model while holding other features constant (Friedman 2001). The same
184 plot can also be used to infer the type of relationship between each feature and the target. A PDP
185 is created by varying the feature of interest across its range, and for each value, we make a
186 prediction using the ML model or codal equation, holding all other features constant at their
187 average values. The average prediction is then plotted against the values of the feature of interest

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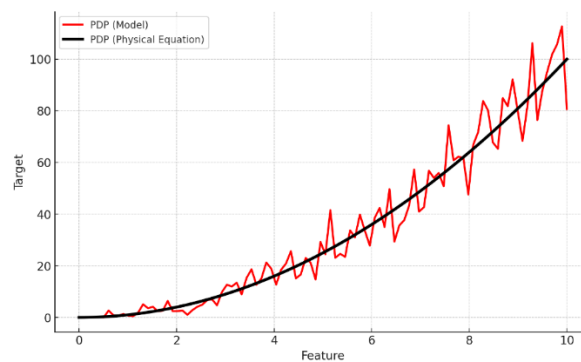
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188 to show the marginal effect of that feature on the predicted outcome. Mathematically, the partial
189 dependence of a model f with respect to a set of features X_S can be defined as:

$$190 \quad PDP_{X_S} = \frac{1}{n} \sum_{i=1}^n f(X_S, X_{C_i}) \quad (2)$$

191 where X_{C_i} are the remaining features for the i -th observation, and n is the number of observations.

192 The key insight behind PDPs is that by averaging out the effects of all other features, then this tool
193 can isolate the effect of the feature of interest. Thereby, the relationship between the target and a
194 feature can be revealed. Fig. 2 illustrates a hypothetical PDP obtained from a ML model and from
195 a physical equation. This PDP can show how changing the feature at hand while keeping all other
196 features constant affects the predicted target. In this figure, one can see that the hypothetical
197 model's PDP has a similar trend and behavior, to some extent, to that of the hypothetical equation.
198 This implies that model and equation predictions are within certain a certain bound (i.e.,
199 percentage).



200
201 Fig. 2 A demonstration of PDPs [Note: the target and feature are assumed to be unitless for
202 demonstration purposes.]

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203 3.3 Equivalence through accumulated local effects (ALE)

204 While PDPs provide valuable insights, they can be biased when features are correlated because
205 PDPs treat features independently. Thus, ALEs are another tool that can be used to explain ML
206 models. However, unlike PDPs, ALEs provide a more accurate representation when features are
207 correlated. For example, ALEs provide a way to visualize feature effects by taking into account
208 the average effects of other features. Hence, ALE plots can be especially useful when there are
209 interactions between features. ALEs handle interactions between features by only considering the
210 local effects; hence they are not biased by global correlations like PDPs. They also are centered
211 around the average prediction over the training data, which makes them easier to interpret in terms
212 of the average prediction.

213 The ALE of a feature is calculated by accumulating its *local effects* (i.e., the difference between
214 the prediction for a slightly higher value of the feature and the prediction for a slightly lower value
215 for the same feature, averaged over the dataset). To calculate ALE, we first divide the feature of
216 interest into intervals. For each interval, we compute the difference in the model's predictions at
217 the upper and lower bounds of the interval while keeping other features constant. This difference
218 is then accumulated across the intervals to obtain the ALE plot. Mathematically, the ALE for a
219 feature x_i can be expressed as:

$$220 \text{ALE}_{x_i} = \frac{1}{n} \sum_{i=1}^n [f(x_{i,j+1}, X_{-i}) - f(x_{i,j}, X_{-i})] \quad (3)$$

221 Where $x_{i,j}$ is the value of feature x_i for the j -th observation, and X_{-i} are the remaining features.

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222 The following example can come in handy to better compare PDPs and ALEs. For example, a PDP
223 might show how the predicted sectional capacity changes with the cross-sectional area while
224 averaging out the effect of the material strength. If there is a strong interaction between the cross-
225 sectional area and the material (e.g., if changing the material significantly affects how the cross-
226 sectional area influences the capacity), this interaction effect could be hidden in a PDP. On the
227 other hand, suppose there is an interaction between the cross-sectional area and the material of the
228 load-bearing member. An ALE plot can capture this interaction by showing the effect of changing
229 the cross-sectional area on the predicted capacity, considering the material feature's average effect.
230 For visualization purposes, both PDP and ALE are quite similar.

231 *3.4 Detailed description of the proposed approach*

232 The key challenge herein is that both PDP and ALE are only generated once model training is
233 completed. In other words, these tools cannot be manipulated during the training process, and there
234 is no direct way to train ML models to yield PDPs and ALEs that fit some criteria. Similarly, the
235 traditional way of tuning model parameters (i.e., hyperparameters) to improve model accuracy
236 cannot be applied herein to arrive at pre-specified PDPs and ALEs. Simply adjusting model
237 parameters directly to match the PDPs and ALEs of the physical equation can be quite challenging
238 because PDPs and ALEs are, as mentioned above, not directly connected to the model's
239 parameters. Therefore, this challenge is inherently nontrivial and would involve creating a loss
240 function that incorporates the discrepancy between the model's PDPs/ALEs and the target
241 PDPs/ALEs and then optimizing this loss function to find the best parameters.

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242 Thus, a new approach is proposed herein. This approach utilizes *learning by indirect feedback*.
243 Rather than adjusting the model parameters directly to fit the PDPs and ALEs of the equation, we
244 will be slightly adjusting the training data based on the discrepancy between the ML model's
245 PDPs/ALEs and the equation's PDPs/ALEs and re-train the model on this adjusted data. Simply,
246 we tune the ML model, and one of the means of tuning the model (among other standard methods
247 often used in ML analyses) includes a step wherein the discrepancy between the PDPs/ALEs is
248 minimized.

249 As will be demonstrated in the to-be-presented case studies, this approach has the potential to
250 guide the ML model to learn the correct behavior (as defined by the PDPs and ALEs of the physical
251 equation) while still being able to fit the actual data. This approach can transfer the embedded
252 empirical scientific knowledge from codal provisions into ML and can be particularly useful in
253 situations where we have a good understanding of the underlying physics or other processes, but
254 the actual data is noisy or incomplete, so a purely data-driven model may not be accurate or
255 reliable. In other words, while a traditionally-trained ML model can achieve high accuracy (as will
256 be shown in the presented case studies), such a model does not generally attain PDPs and ALEs
257 that match those from codal provisions. However, the proposed approach ensures that a ML will
258 realize matching PDPs/ALEs and high predictive accuracy.

259 More specifically, the proposed approach entails the following steps:

- 260 1. Training an initial ML model and then calculating the PDP and ALE for each feature.
- 261 2. Then, computing the differences between the PDPs and ALEs of the model and those of
262 the equation an engineer want the model to match.

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263 3. The calculated differences are then used to adjust the target variable by iterating over each
264 unique value in a feature and adjusting the target variable for all instances with a feature
265 value in a certain interval.

266 4. The adjustment is calculated as the product of the learning rate (calculated using a decay
267 formula = $learning\ rate / (1 + decay\ rate \times iteration)$), the difference in PDPs or
268 ALEs, and a sensitivity parameter that represents how sensitive the target is to changes in
269 this feature.

270 ○ More specifically, The adjustment is calculated as follows:

271
$$adjustment_{pdp} = learning\ rate_{pdp} \times pdp\ difference[i] \times sensitivity_{pdp}$$

272
$$adjustment_{ale} = learning\ rate_{ale} \times ale\ difference[i] \times sensitivity_{ale}$$

273 ○ Here, $Learning\ rate_{pdp}$ and $learning\ rate_{ale}$ are the learning rates for the PDP and
274 ALE, respectively, calculated using a decay formula, which measures how quickly
275 the model should adjust its predictions based on the differences. $pdp\ difference[i]$
276 and $ale\ difference[i]$ represent the absolute difference between the model's
277 PDP/ALE and the equation's PDP/ALE for the current feature value. $sensitivity_{pdp}$
278 and $sensitivity_{ale}$ are the sensitivities of the output to the feature for PDP and ALE,
279 respectively. These measure how much the output changes with respect to a small
280 change in the feature. The adjustments are then applied to the target values ('FR')
281 in the training data where the feature value is between the current value and the
282 next value.

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- 283 5. This adjustment is then added to the target variable for all instances where the feature value
284 falls within a certain range.
- 285 6. The process is repeated until the maximum number of iterations (default is set to 100) is
286 satisfied or until the differences between the model's PDPs and ALEs and the equation's
287 PDPs and ALEs fall below a certain similarity threshold as defined per each measure.
- 288 ○ If the model's PDPs/ALEs are similar to the equation effect's PDPs/ALEs (as per
289 the predefined similarity measures), the process continues to the next feature. If not,
290 the targets in the training data are adjusted based on the differences, and the model
291 is re-trained.
- 292 ○ If similarity is not achieved for all features within the maximum number of
293 iterations, the algorithm moves on to the next measure.
- 294 7. After looping over all measures, a similarity check is examined to verify if the similarity
295 was achieved for all features for all measures.
- 296 ○ If so, each model that satisfies a specific measure is retained.
- 297 8. Finally, an ensemble model is created using all the retained models. The PDP and ALE for
298 the ensemble model are calculated. This ensemble model, therefore, represents a
299 combination of models, each trained for a different measure and adjusted for each feature,
300 based on the differences between the model's PDPs/ALEs and the equation's PDPs/ALEs.

301 As one can see, there are three main loops, a similarity measures loop, an iteration loop, and a
302 feature loop. Depending on the scenario at hand, an engineer can opt to choose if each loop needs
303 to satisfy one/all measures, iterations and/or features. Similarly, the number of iterations may need

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304 to be adjusted per problem/equation. After testing this approach for a number of problems, it
305 became clear that a balance across the three loops is to be accomplished. In most cases, arriving at
306 an ensemble with models satisfying 2-3 measures, all features, and within the maximum number
307 of iterations seems to yield balanced results. Additional testing and verification are likely to
308 continue in the future.

309 *3.5 Similarity measures*

310 As mentioned above, the relationships between features in building codes are governed by physical
311 equations/provisions. Thus, if a ML model is developed to mimic these physical processes, then
312 PDP and ALE of the model need to also mimic the logic of the physical equation. The elemental
313 idea here is that if the PDP and/or ALE of a feature in the model follows the same trend as the
314 physical equation, this implies that the ML model has learned the underlying engineering intuition
315 and causal logic of the physical process. For example, if the physical equation describes a linear
316 relationship between a feature and its target, and the PDP or ALE of these variables in the model
317 also shows a linear relationship, this would suggest that the model has learned this relationship.

318 Now, we move to present the selected similarity measures. These measures were selected to be
319 largely independent of each other to maximize their strengths and minimize their limitations. The
320 derivation of these measures can be found in their respective works cited below.

321 3.5.1 Normalized Euclidean distance

322 The normalized Euclidean distance function calculates the Euclidean distance between two vectors
323 and then normalizes this distance by the number of elements in the vectors (see Fig. 3) (Bernardin
324 et al. 2017). Normalizing the distance by the number of elements is a way to make this measure

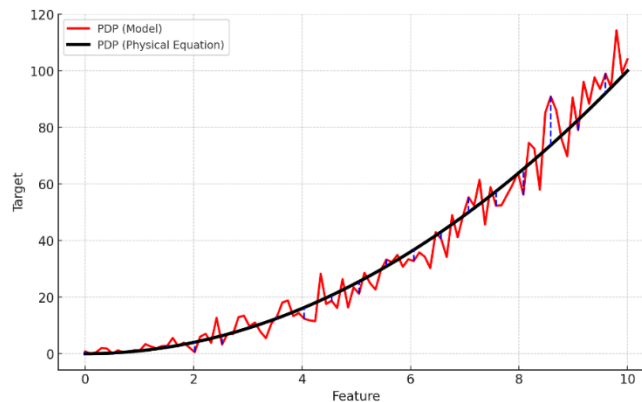
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325 scale independent. This can be useful when comparing distances across datasets with different
326 numbers of elements. The Euclidean distance is the straight-line distance between two points in
327 space and is calculated as:

$$328 \quad d(p, q) = \sqrt{(p_1 - q_1)^2 + \dots + (p_n - q_n)^2} \quad (4)$$

329 where p and q are two points in an n -dimensional space. This measure returns a zero if the shapes
330 are identical and unity when completely dissimilar (the default setting was arbitrarily chosen as
331 0.25 in this study).



332
333 Fig. 3 Illustration of the normalized Euclidean distance measure (presented in dashes)

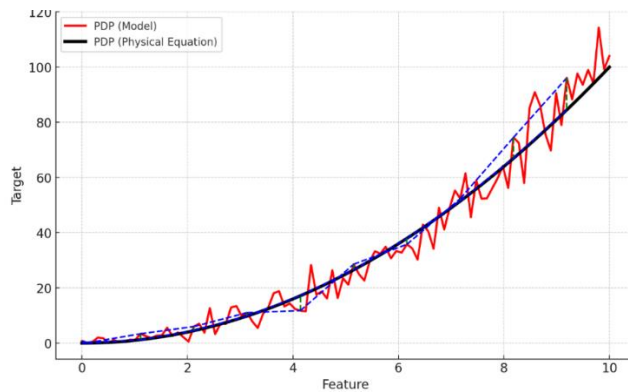
334 3.5.2 Fréchet distance

335 The Fréchet distance is another measure of similarity between two curves that takes into account
336 the location and ordering of the points along the curves (Aronov et al. 2006). This measure is
337 formally described as the length of the shortest leash required to let a pet and its owner walk along
338 their separate paths, where the pet and the owner can vary their speed but cannot go backward (see
339 Fig. 4). The Fréchet distance function implemented here calculates the discrete Fréchet distance
340 between two curves, represented as arrays, and results in a single value (with the same units as the

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341 target value) representing the similarity between the two curves. This measure assumes that the
342 curves are continuous and connected and that the order of points along the curve matters. Since
343 this measure returns similarity in the same units as the target, a default setting was arbitrarily
344 chosen as 10% of the observed target observation in this study).



345
346 Fig. 4 Illustration of the Fréchet distance measure (presented in dashes)

347 3.5.3 Bounding measure

348 The custom bounding measure calculates an upper and a lower bound based on a specified
349 threshold (see Fig. 5). The idea is to determine whether the PDP/ALE values from the ML model
350 fall within a certain range of values defined by a physical equation. The measure returns the
351 proportion of model values that fall within the bounds. This measure assumes that the physical
352 equation provides a ground truth range of acceptable values. One should note that the choice of
353 threshold is arbitrary (taken as 10% in this study) and that this measure does not take into account
354 the order of the values.

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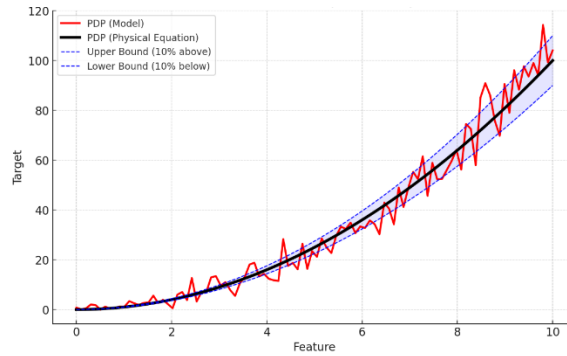


Fig. 5 Illustration of the bounding measure (presented in dashes)

3.5.4. Coefficient of determination and correlation coefficient

In addition to the above four measures, two commonly used statistical measures can be used to establish similarity between PDPs or ALEs of a model and a physical equation: the R^2 (coefficient of determination) and the correlation coefficient (r) are also used. The R^2 represents the proportion of the variance for a dependent variable that is explained by a number of features in a model. The r , on the other hand, measures the strength and direction of a linear relationship between two variables. In the context of comparing PDPs or ALEs of a model and a physical equation, a high R^2 or r approaching unity would suggest a high degree of similarity. A similarity of more than 70% was deemed to be strong, as noted in (Smith 1986).

$$R^2 = 1 - \frac{\sum_{i=1}^n (P_i - A_i)^2}{\sum_{i=1}^n (A_i - A_{mean})^2} \quad (5)$$

$$R = \frac{\sum_{i=1}^n (A_i - \bar{A}_i)(P_i - \bar{P}_i)}{\sqrt{\sum_{i=1}^n (A_i - \bar{A}_i)^2 \sum_{i=1}^n (P_i - \bar{P}_i)^2}} \quad (6)$$

where, A : actual measurements, P : predictions, n : number of data points.

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369 *3.6 Machine learning models*

370 Five ML algorithms were used herein, and these were selected as they are commonly used
371 algorithms in our domain, as noted in a recent survey (Tapeh and Naser 2022). All ML algorithms
372 are used in their default settings (including hyperparameters) for transparency and to allow
373 repetition of the proposed approach. The following sections briefly describe such algorithms, and
374 their full description and scripts can be found in their respective references, as cited below. The
375 specific script used in creating the provided analysis can be requested from the author.

376 3.6.1 Decision trees (DT)

377 A decision tree is a supervised ML algorithm that uses a tree-like graph of decisions and their
378 possible consequences (Naser 2021a). It is a flowchart-like structure, where each internal node
379 denotes a test on a feature, each branch represents an outcome, and each leaf node holds a class
380 label. The process of constructing a decision tree involves selecting features to test at each node in
381 the tree to minimize the total variance of the target variable among the instances at each node.
382 There are several strategies for making this choice, but a common one is to use information gain,
383 which is related to the concept of entropy (a measure of impurity) (Kent 1983).

384 3.6.2 Random Forest (RF)

385 Random Forest (RF) is a versatile ensemble learning algorithm that combines the power of
386 decision trees and randomization techniques (Breiman 2001). The RF algorithm constructs an
387 ensemble of decision trees by randomly selecting subsets of the training data and features. The
388 individual trees are trained independently using the selected subsets, and their predictions are
389 aggregated to produce the final prediction. Each decision tree in the RF ensemble is built using a

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390 random subset of the training data (known as bootstrap aggregating or bagging). This random
391 sampling process helps to reduce the risk of overfitting and improves the model's generalization
392 ability. Additionally, the algorithm selects a random subset of features at each split in the tree
393 construction, introducing diversity among the trees and reducing the impact of individual features.

394 3.6.3 Extreme gradient boosted trees (XGboost)

395 XGBoost is based on the gradient boosting framework (Scikit 2020; XGBoost Python Package
396 2020). Gradient boosting is a method that goes through cycles to iteratively add models into an
397 ensemble. It begins by initializing an ensemble with a single model, whose predictions can be
398 pretty naive. Then, the algorithm begins to add new models that aim to correct the errors of the
399 combined ensemble. In this way, the models are added sequentially until no further improvements
400 can be made. One of the main improvements that XGBoost brings for tree-like models is a more
401 regularized model formalization to control overfitting, which tends to be a problem with gradient
402 boosting.

403 3.6.4 Light gradient boosting machine (LGBM)

404 The Light Gradient Boosting Machine (LGBM) is an improvement over the XGboost as it
405 combines the strengths of gradient boosting and the LightGBM framework to achieve high
406 performance (Ke et al. 2017). This optimizes the objective function by iteratively fitting new trees
407 to the negative gradient of the loss function with respect to the current predictions. The final
408 prediction is obtained by summing the predictions of all the trees. The exclusive feature bundling
409 technique in LGBM groups data points in a near-lossless way, leveraging similarities within the

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410 data. This technique improves computational efficiency by reducing the number of distinct feature
411 values and enabling efficient memory usage during the training process.

412 3.6.5 Support Vector Machines (SVM)

413 The Support Vector Machines (SVM) algorithm aims to find the optimal hyperplane that
414 maximally separates the data points (Scikit n.d.). The objective is to minimize the deviation or
415 error between the actual data points and the hyperplane while considering the regularization
416 parameters. To handle non-linearly separable data, SVM utilizes kernel functions to transform the
417 input data into a higher-dimensional feature space where it becomes linearly separable.

418 *3.7 Performance metrics*

419 Once the ensemble is created. This ensemble is trained by randomly shuffling and training the data
420 into training (T), validation (V), and testing (S) sets. The ensemble is trained and validated against
421 the T and V sets and then examined on the S set following a k-fold cross-validation procedure,
422 wherein the collected dataset was randomly split into test and training sets of $k = 10$ groups. The
423 ensemble is trained using nine unique sets and validated on the tenth remaining set until each
424 unique set is used as the validation set.

425 Then, in lieu of the above discussed measures selected to verify and compare the similarity
426 between the PDPs/ALEs of the ML model and codal provision, the validity of the created ML
427 models is also examined through another independent performance metric, namely, the Mean
428 Absolute Error (MAE) as listed below, as well as R^2 (Naser et al. 2021; Tapeh and Naser 2022).

$$429 \quad MAE = \frac{\sum_{i=1}^n |P_i - A_i|}{n} \quad (7)$$

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430 **4.0 Case Studies**

431 Seven phenomena and their respective codal provisions are used herein to showcase and verify the
432 proposed methodology. These are presented in the order of their complexity (i.e., the number of
433 involved features). Two phenomena are taken from ACI 318 (Building Code Requirements for
434 Structural Concrete and Commentary). Two phenomena were curated from ASCE29 (Standard
435 Calculation Methods for Structural Fire Protection), wherein one phenomenon also appears in the
436 Technical Report no. 10 by the National design specification (NDS) for wood construction. The
437 fifth phenomenon is taken from the Australian Building Code (AS3600) for concrete construction.
438 The sixth case study is taken from the American Institute of Steel Construction (AISC) Steel
439 Construction manual. The final case study is present in multiple building codes as it deals with the
440 elastic deformation of beams.

441 Each phenomenon was examined with data that satisfies the practical range of the codal provision
442 at hand, and this data also satisfy the recommendations of the recent researchers aimed to establish
443 the health of data (Van Smeden et al. (Smeden et al. 2018) with a minimum set of 10 observations
444 per feature, Riley et al. (Riley et al. 2019) with a minimum set of 23 observations per feature, and
445 Frank and Todeschini (Frank and Todeschini 1994) with a minimum ratio between the number of
446 observations and features as 3 and 5). In addition, a random ML algorithm from those listed earlier
447 was selected for each case study to create the tuned ensemble, and the other algorithms were used
448 without tuning (i.e., without being incorporated into the proposed equivalence approach) for
449 comparison. The rationale behind the decision is to show the proposed approach's wide
450 applicability and maintain the page limitation of this work, as examining each individual ML

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451 model for each case study pushed the size of this paper beyond what is commonly expected. All
452 case studies used the default settings listed above. In the upcoming PDP and ALE figures, the
453 reader must remember that the vertical axis represents the partial and accumulated effects on the
454 target instead of the target itself.

455 *4.1 ACI318: Code Section 19.2.3.1 on modulus of rupture*

456 In the context of building design and construction, the tensile strength of concrete is particularly
457 important as it helps to determine the concrete's ability to resist tensile and torsional forces, as well
458 as cracking (say due to environmental factors like temperature changes and freeze-thaw cycles,
459 etc.). The tensile strength of concrete is generally only about 10% of its compressive strength and
460 measures the force required to break/crack concrete.

461 Although the tensile strength of concrete increases with an increase in the compressive strength,
462 the ratio of the tensile to the compressive strength decreases as the latter strength increases. The
463 tensile strength is often approximated proportionally to the square root of the compressive strength
464 of concrete. More specifically, ACI 318 Code Section 19.2.3.1 the modulus of rupture for normal
465 strength concrete for use in calculating deflections as obtained from statistical analysis (see
466 (McNeely and Stanley 1963; Raphael 1984)):

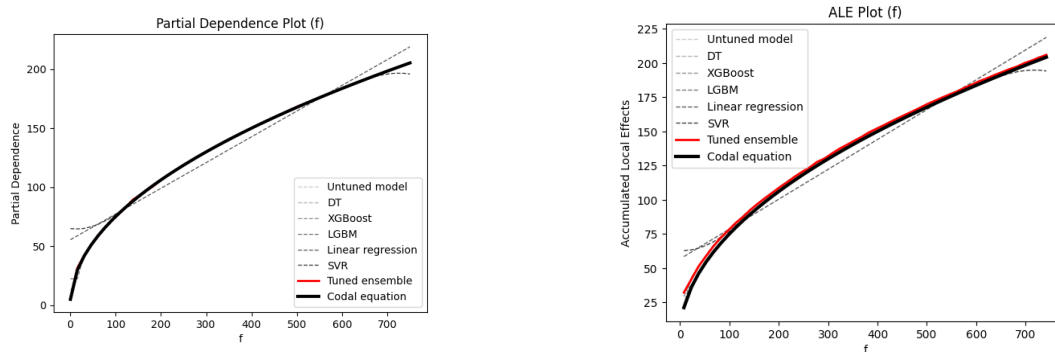
$$467 \quad f_r = 7.5\sqrt{f'_c} \quad (8)$$

468 As one can see, this is a simple statistical equation and presents a suitable candidate for a first case
469 study. Thus, the presented approach above will be applied to creating a ML ensemble that mimics
470 this equation. Due to the simplicity of this problem, one similarity measure (normalized Euclidean

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471 distance) was used. Upon the successful tuning of the ensemble, the $R^2_{ensemble}$ was unity and
472 $MAE_{ensemble}$ was calculated at 0.192, and the same metric, when calculated for the RF (without
473 tuning), was at 0.203, implying a 5.4% improvement in accuracy. The outcome of this approach
474 is presented in Fig. 6. This figure shows that the PDP and ALE of the equivalent ensemble (made
475 from RF) match well throughout the full series with the above codal equation. It is also worth
476 noting that the PDPs and ALEs from all tree-based algorithms also matched those of the codal
477 equation well. This can indicate that such models can predict this phenomenon without actually
478 being tuned. This working hypothesis is being examined at the moment in a separate work and, at
479 the time of this work, appears to be true for simple phenomena.



480 Fig. 6 Comparison for case study no. 1(in psi) [Note: f denotes the compressive strength of
481 concrete. The base ML mode: RF.]

482 4.2 ASCE29: Standard Section 3.3 on the design of fire-resistive exposed wood members

483 ASCE 29 is a standard for calculating the fire resistance of structural members and barrier
484 assemblies made from structural steel, un/reinforced concrete, timber, and masonry and is
485 developed as a joint effort between ASCE's Structural Engineering Institute and the Society of Fire

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486 Protection Engineers (SFPE). This standard contains a number of empirical codal provisions that
487 can be used to evaluate/predict the fire resistance of structural members.

488 Sec. 3.3 in this standard provides guidance on calculating the fire resistance rating (or time to
489 failure in minutes, t), measured in minutes, of timber beams with a least nominal dimension of 6
490 in. (or 140 mm). For the severe case of beams exposed on four sides, t , is calculated as:

$$491 \quad t = \gamma z b [4 - (b/d)] \quad (9)$$

492 where, γ is a constant (2.54 min/in. or 0.1 min/mm), z is the load factor equals 1.3 for lightly loaded
493 beams with a ratio $< 50\%$, b and d are the actual breadth and depth of a beam. It is worth noting
494 that the same empirical equation also appears in the Technical Report no. 10 by the National
495 Design Specification (NDS) for wood construction (NDS 2018). As one can see, this empirical
496 expression contains four parameters, two of which are considered constants and hence are treated
497 as such, and hence only b and d are considered as features. This case study applied the proposed
498 methodology by using LGBM as the base ML model.

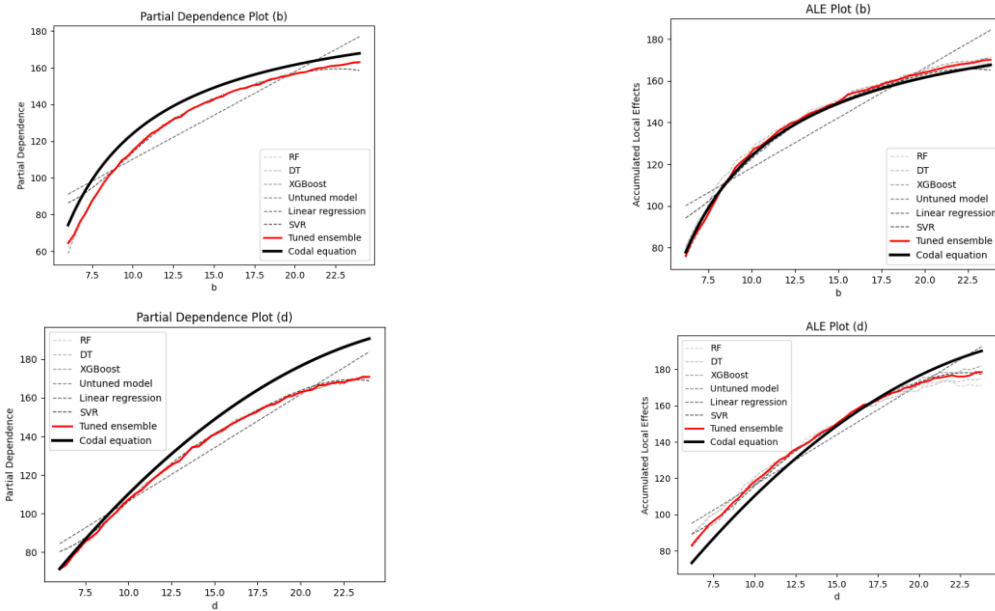
499 In this case study, only three similarity measures converged with default settings (i.e., Fréchet
500 distance, the Bounding measure, and the normalized Euclidean distance). Special tuning was not
501 applied to converge the other measure as the realized results were deemed acceptable (see Fig. 7).

502 The $MAE_{ensemble}$ was calculated at 0.859 min, and the same metric, when calculated for the same
503 algorithm (without tuning), was at 1.111 min. R^2 between the ensemble and the codal equation was
504 unity. It is clear that the tuned ensemble outperforms all individual models in matching the codal
505 equation's PDPs and ALEs. In this case study, and as shown in the next study, matching PDPs is
506 often seen to be faster (and affordable) than matching ALEs. This stems from the more complex

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507 derivation nature of ALEs compared to PDPs. Given this observation, the proposed methodology
 508 was appended to allow the user/engineer to select if they seek to match PDP, ALE, or both. Such
 509 an amendment did not alter the analysis shown in the first case study.



510 Fig. 7 Comparison for case study no. 2 (in min) [Note: b and d denote the breadth and depth of
 511 timber beams, respectively. The base ML mode: LGBM.]

512 *4.3 ACI318: Table 22.5.5.1 on shear strength for beams without minimum shear reinforcement*

513 ACI Code Table 22.5.5.1 lists the following equation for calculating the shear strength for beams
 514 without minimum shear reinforcement. This equation results from an iterative process led by the
 515 Joint ACI-ASCE Committee 445 and Subcommittee E of ACI Committee 318.

$$516 V_c = [8\lambda_s\lambda\rho^{1/3}\sqrt{f_c} + N_u/6A_g]bd \quad (10)$$

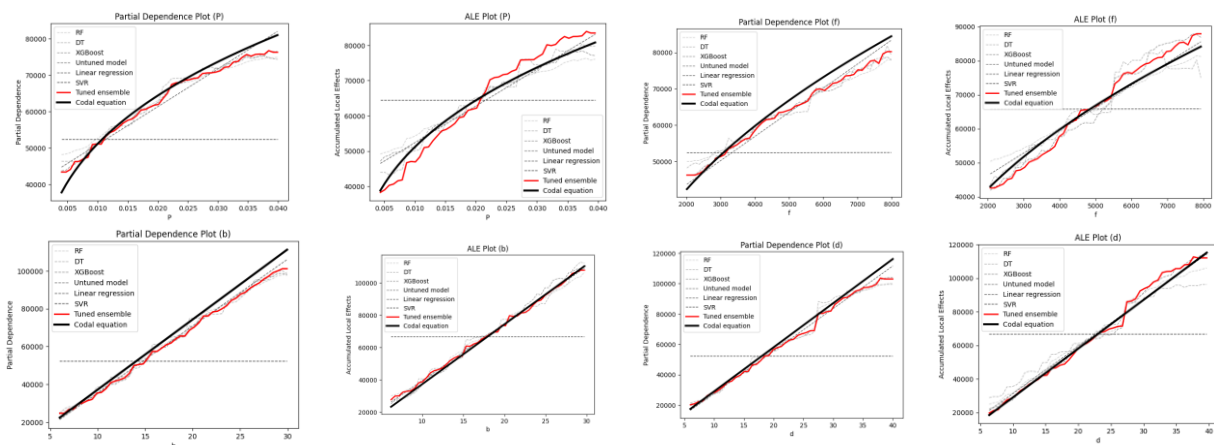
517 where ρ_w is the flexural reinforcement ratio for tension reinforcement in a section of A_s/b_wd , N_u is
 518 the member-factored axial load, and A_g is the gross member area. The lightweight-aggregate

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519 concrete factor, λ , was defined previously. The value of V_c shall not be taken as less than zero, nor
 520 as greater than $\lambda 5 (f'_c)^{0.5} b_w d$, and $N_u/6A_g$ shall not be taken as greater than $0.05f'_c$. In this case
 521 study, beams with applied axial forces were not considered. In addition, λ_s (size effect term) and λ
 522 were taken as unity for simplicity.

523 The LGBM was used in this case study as the base model. Figure 8 shows the behaviour of the
 524 tuned ensemble in terms of PDPs and ALEs after satisfying two similarity measures, namely the
 525 Fréchet distance and the Bounding measure. The $MAE_{ensemble}$ was calculated at 3444.348 lbs and
 526 at 3620.0 lbs for the untuned model. The R^2 for the ensemble was 99%. Clear matching between
 527 the ensemble and codal equation is evident.



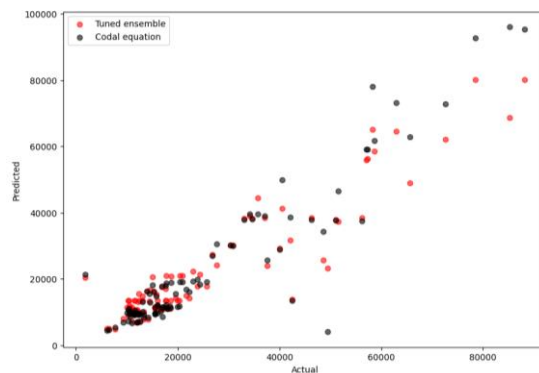
528 Fig. 8 Comparison for case study no. 3 (in lbs) [Note: The base ML mode: LGBM.]

529 To further examine the performance of the tuned ensemble (as well as the proposed approach), an
 530 additional layer of validation is followed herein. In this process, 100 random beams were selected
 531 from ACI's shear database (Reineck et al. 2003) for reinforced concrete members without shear
 532 reinforcement used in deriving the codal expression were examined against the codal expression
 533 and tuned ensemble. Figure 9 shows the results of this comparison and notes that the ensemble

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534 achieves a better predictive capability than the codal expression in predicting the shear strength of
535 the selected beams ($MAE_{ensemble} = 4930.51$ lbs, $MAE_{codalexpression} = 5219.73$, $R^2_{ensemble} = 84.1\%$ and
536 $R^2_{codalexpression} = 80.83\%$). It is worth noting that this additional external verification was not
537 possible to conduct in the other case studies as the data used to create the codal provisions of
538 interest were not available.



539

540 Fig. 9 Comparison against 100 randomly selected beams from ACI's shear database (in lbs)

541

[Note: the database is accessible in (Reineck et al. 2003)]

542

4.4 ASCE29: Standard Section 5.2.3 on concrete-filled hollow steel columns

543

Another complex codal provision is tackled in this case study. The ASCE29 also presents guidance

544

on evaluating the fire resistance rating of hollow steel columns filled with unreinforced normal

545

weight concrete through the following provision. This equation was established empirically

546

through a number of publications and has been verified by computer simulations at the National

547

Research Council of Canada (NRC) (Kodur 1999; Kodur and MacKinnon 2000). It is worth noting

548

that this expression is also listed under Sec. D-2.6.6. in the National Building Code of Canada and

549

is also applicable to tubular shapes; however, only the case of circular tubes is presented herein.

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$$R = a \frac{(f+20)}{60(L_e-1000)} D^2 \sqrt{D/C} \quad (11)$$

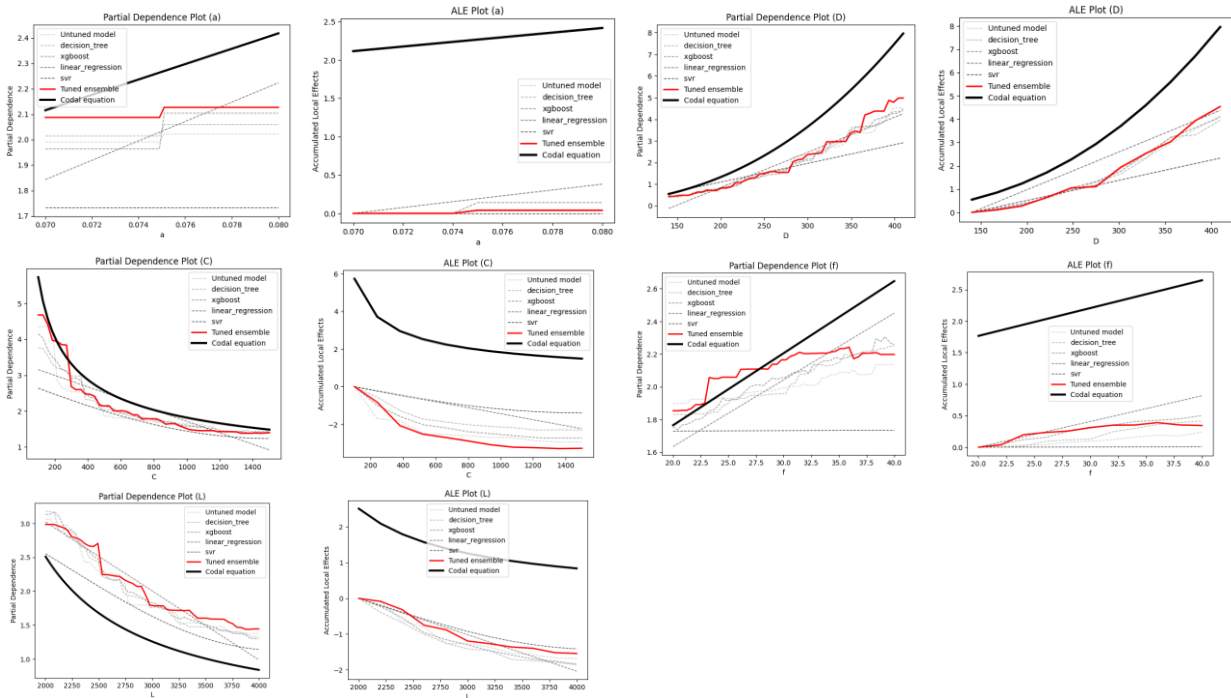
550 where, R is the fire resistance rating in hours, a is 0.07 for circular columns filled with siliceous
551 aggregate concrete, and 0.08 for circular columns filled with carbonate aggregate concrete. f is
552 the specified 28-day compressive strength of concrete (MPa), L_e is the column effective length
553 (mm), D is the outside diameter for circular columns (mm), and C is the compressive force due to
554 the unfactored dead load and live load in kips (kN).
555

556 This codal provision is accompanied by additional stipulations that were enforced in this analysis,
557 including, the required R rating shall be less than or equal to 2 hours, the specified f shall be equal
558 to or greater than 20 MPa and shall not exceed 40 MPa. the column's effective length shall be at
559 least 2000 mm and shall not exceed 4,000 mm, the outside diameter shall be at least 140 mm and
560 shall not exceed 410 mm, and the compressive force shall not exceed the design strength of the
561 concrete core determined in accordance with AISC LRFD-94, "Load and resistance factor design
562 specification for structural steel buildings."

563 The RF algorithm was used as the base model. The convergence of the ensemble on the PDPs and
564 ALEs was difficult to obtain, and hence the presented results in Fig. 10 are shown for a converged
565 run wherein only the PDPs were matched using all aforementioned similarity measures were
566 satisfied. Despite only matching the PDPs, the ALEs seem to also attain some degree of matching
567 resemblance to that from the equation. The $MAE_{ensemble}$ was calculated at 0.281 hours and at 0.471
568 hours for the untuned model – an improvement of about 40%.

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569 Fig. 10 Comparison for case study no. 4 (in hours) [Note: The base ML mode: LGBM.]

570 4.5 AS3600 Fire resistance of concrete columns

571 This case study tackles a more complex codal provision with six variables. A former edition of the
 572 Australian concrete code (AS3600) homed the following statistical-based codal equation to
 573 evaluate the fire resistance of concrete columns (Wade et al. 1997). This equation was fitted using
 574 the results of standard fire tests and numerical simulations.

575
$$R = \frac{k \times f^{1.3} \times B^{3.3} D^{1.8}}{10^5 \times N^{1.5} \times L^{0.9}} \quad (12)$$

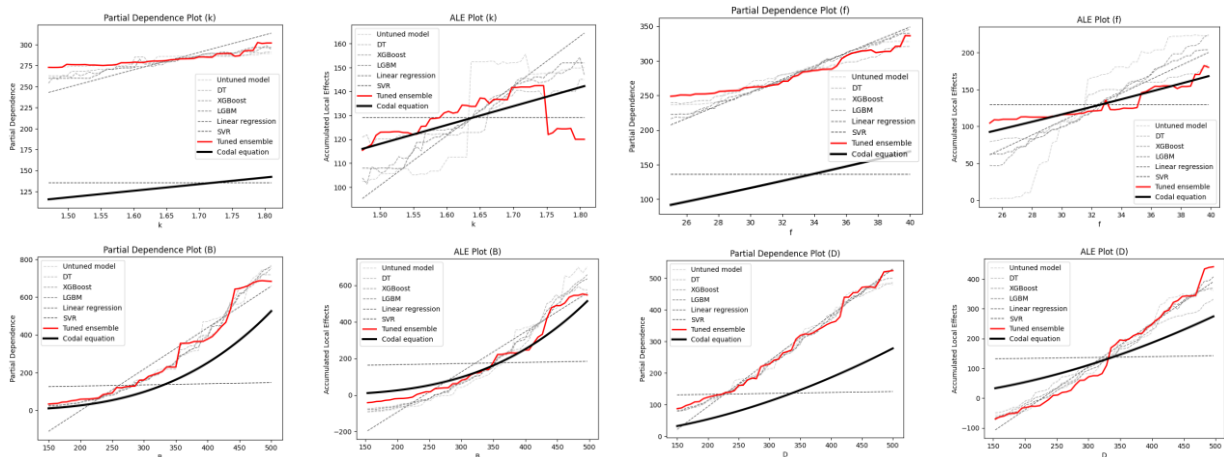
576 where, R is the fire resistance (min), k is the constant dependent on cover and steel reinforcement
 577 ratio (equals to 1.47 and 1.48 for a cover less than 35 mm and greater than or equal to 35 mm,
 578 respectively), f_c is the 28-day compressive strength of concrete (MPa), B is the least dimension of

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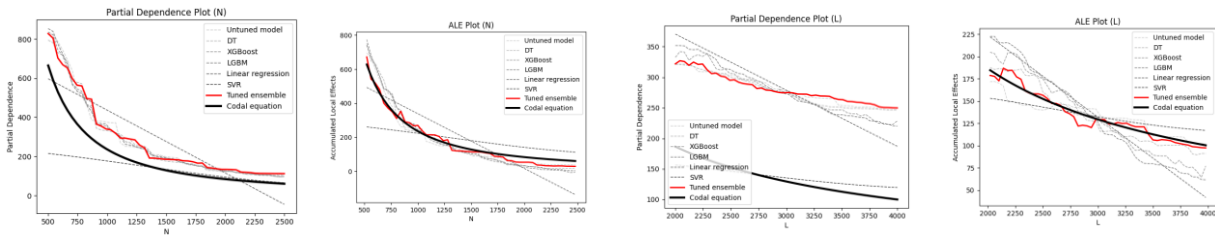
579 column (mm), D is the greatest dimension of column (mm), N is the axial load during fire (kN),
 580 and L is the effective length (mm).

581 This case study utilizes the RF algorithm as a base model. In addition, R^2 and the bounding measure
 582 were satisfied in this case study. The $MAE_{ensemble}$ (with default settings) was calculated at 56.957
 583 min, and the same metric, when calculated for the same algorithm (without tuning), was at 68.03
 584 min (R^2 between the ensemble and the codal equation was 89%, and it is quite possible to improve
 585 the performance of the tuned ensemble by tuning the default settings). The tuned ensemble seems
 586 to match a good degree of similarity in terms of trends between PDPs and ALEs with the former
 587 codal provision (see Fig. 11). In some features (namely, k , f , and L), a gap is noticed to occur
 588 between the PDPs and ALEs obtained from all ML Models and the untuned equation. This gap seems to
 589 have a shifting effect, wherein the models capture the trends of the PDPs/ALEs but not the values
 590 in some of the involved features.



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591 Fig. 11 Comparison for case study no. 3 (in min) [Note: b and d denote the breadth and depth of
592 timber beams, respectively. The base ML mode: LGBM.]

593 *4.6 Additional case studies based on provisions stemming from a theoretical derivation*

594 These two case studies explore the applicability of the proposed approach to codal provisions that
595 are not empirical in nature but rather derived from first principles.

596 AISC: Manual Section F6.1. for I-shaped members and channels bent about their minor axis

597 Section F6.1 in the AISC manual presents the following simple equation to evaluate the nominal
598 flexural strength, M_n , in yielding.

599
$$M = f_y \times Z \leq 1.6 f_y S_y \tag{13}$$

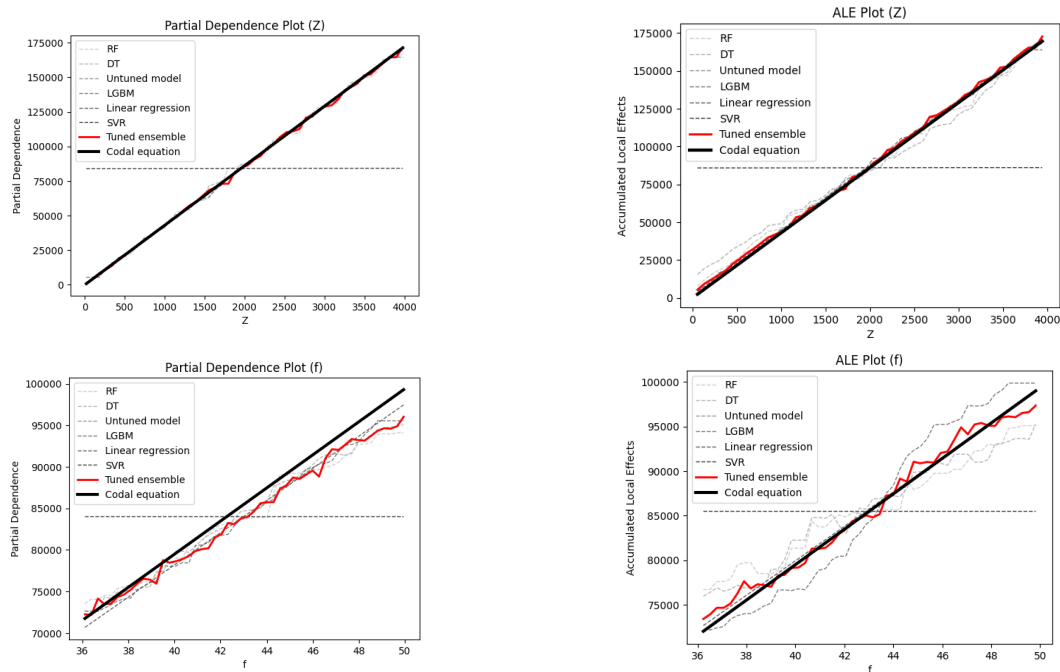
600 where, S_y is the elastic section modulus taken about the y-axis.

601 This simple codal provision has two main features, and the data used in this case study were
602 selected to satisfy the noted condition. XGBoost was selected to be the base ML model with two
603 similarity measures (i.e., Fréchet distance and the Bounding measure). The outcome of this
604 analysis is shown in Fig. 12. Both similarity metrics were satisfied, and the $MAE_{ensemble}$ was
605 calculated at 1637.95 kip.in, and the same metric, when calculated for the same algorithm (without
606 tuning), was at 1659.74 kip.in. Looking at Fig. 12 clearly shows that the tuned ensemble matches
607 the PDP and ALE of the codal equation and outperforms those obtained from the other models.

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608 Despite being a simple case study and the need for additional tests to come in future work, this
 609 finding seems to indicate the suitability and applicability of the proposed approach to the ability
 610 of ML to mimic principle-based codal provisions.



611 Fig. 12 Comparison for case study no. 6 (in kip.in) [Note: The base ML mode: XGBoost.]

612 Various building codes: On the elastic deformation of beams

613 Here, another theoretically derived expression is used as a case study. The equation for elastic
 614 deformation in simply supported beams loaded with a point load placed at the midspan is shown
 615 below and can be found in a variety of building codes/standards (such as Table 3-23 in the AISC
 616 manual):

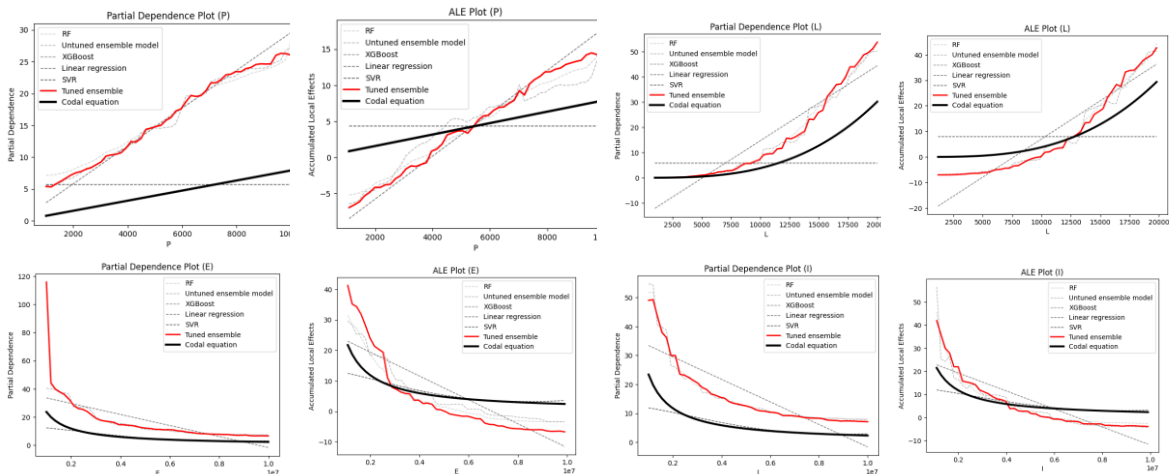
617
$$\text{Elastic deformation} = \frac{PL}{48EI} \tag{14}$$

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618 where, P is the applied load (N), L is the span of the beam (mm), E is the modulus of elasticity
 619 (Pa), and I is the moment of inertia (mm^4).

620 For this case study, the XGBoost model was selected as the base model. All five similarity
 621 measures were used, but only one measure (R^2) was satisfied (given default settings). Figure 13
 622 paints a comparison between the generated PDPs and ALEs from the model and the above
 623 equation. Despite satisfying one similarity measure, the achieved performance can be deemed
 624 acceptable. For completion, the $MAE_{ensemble}$ was calculated at 2.461 mm, and the same metric was
 625 2.391 mm when calculated for the same algorithm (without tuning). R^2 between the ensemble and
 626 the equation was 96%.



627 Fig. 13 Comparison for case study no. 7 (in mm) [Note: The base ML mode: XGBoost]

628 5.0 Additional thoughts, limitations, and future directions

629 This section documents some of the main limitations of the proposed methodology and shares
 630 insights into future research directions.

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631 *5.1. A note on other matching methods*

632 An engineer might entertain the idea of achieving equivalence through matching feature
633 importance (e.g., a measure of how valuable a feature is in the construction of the model) between
634 the codal provision and the ML model. For example, if a given model's error increase after
635 systematically permuting a feature, then the so-called feature is indeed important since permuting
636 has adversely affected the model's predictions (Altmann et al. 2010).

637 While this concept could be possible to integrate into the proposed methodology and was indeed
638 successful in the first two studies (yet, these results were not shown in the body of this work), one
639 must keep in mind that feature importance measures the total effect of shuffling a feature on
640 prediction accuracy. While this is a common approach in ML, the perception of feature importance
641 in an equation is somewhat of a nuanced concept simply because all features in a given equation
642 are necessary to hold true (Naser 2023a). Therefore, one could argue that all features in an equation
643 are equally important.

644 The reader is to note that other explainability measures (i.e., SHAP (SHapley Additive
645 exPlanations (Lundberg and Lee 2017)), LIME (Local Interpretable Model-agnostic Explanations
646 (Ribeiro et al. 2016)), prototypes, etc.) could be explored to build upon the current analysis. The
647 author believes that, despite their computational complexity, such measures could be proven
648 successful and hence can be streamlined and added to the proposed methodology. The author
649 would like to point out that there is room to investigate the influence of model type (i.e., tree-
650 based, ANN, etc.) vs. the degree of explainability. It is possible that some models might fit a

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651 phenomenon more easily/accurately/with higher explainability than other models, as such, there is
652 a possibility of a trade-off between accuracy & explainability.

653 *5.2. Limitations of the proposed methodology and future directions*

654 It is important to note that the presented approach can be viewed as complex and somewhat
655 lengthy. As such, this approach may struggle to guarantee the convergence of a ML model that
656 both fits the data well and matches the physical equation's behavior. In reality, the proposed
657 approach converged within 2 minutes of analysis for all the case studies mentioned in this work
658 using a typical desktop that can be found at a common engineering design office. However, in
659 lengthy simulations or multi-phased codal provisions, it is possible that the proposed approach
660 might suffer from instability due to chasing a target that continues to slightly but constantly
661 changes based on the model's own performance.

662 Fortunately, there are potential solutions to the above problems. One potential approach to attempt
663 to optimize model parameters via gradient-based methods by computing the gradients of the
664 PDPs/ALEs concerning the model parameters. Alternatively, an engineer might consider
665 employing evolutionary or population-based optimization algorithms to search the parameter
666 space for a set that minimizes the discrepancy between the PDPs/ALEs. If neural networks are
667 used, then pre-specified layers can be trained to satisfy similarity metrics separately. Once a layer
668 passes the similarity check, it can then be frozen to maintain it before moving into another measure.
669 This approach could be an alternative to the ensemble approach used herein. It would be interesting
670 to see what other possible solutions (and limitations) this research area might realize in the future.

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671 **6.0 Conclusions**

672 Building codes provide definitive standards to guide civil engineering practices and ensure safety.
673 While ML has shown the potential to enhance predictive abilities, its integration into building
674 codes is complicated due to transparency and regulatory approval issues. As civil engineering
675 moves towards a more data-centric future, blending traditional engineering wisdom with
676 innovative ML approaches could unlock new frontiers in designing and constructing safer, more
677 efficient buildings. This work proposes an approach to modernizing building codes via ML. In this
678 approach, empirical and regression-based codal equations can be used to create equivalent ML
679 models that retain the logic and properties of such equations. This approach has been shown to be
680 successful in structural and fire engineering phenomena homed in notable codal provisions.

681 **Data Availability**

682 Some or all data, models, or code that support the findings of this study are available from the
683 corresponding author upon reasonable request.

684 **Conflict of Interest**

685 The author declares no conflict of interest.

686 **Acknowledgment**

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689 **References**

690 Aladsani, M. A., Burton, H., Abdullah, S. A., and Wallace, J. W. (2022). "Explainable Machine
691 Learning Model for Predicting Drift Capacity of Reinforced Concrete Walls." *ACI*
692 *Structural Journal*.

Please cite this paper as:

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- 693 Altmann, A., Toloşi, L., Sander, O., and Lengauer, T. (2010). “Permutation importance: A
694 corrected feature importance measure.” *Bioinformatics*.
- 695 Aronov, B., Har-Peled, S., Knauer, C., Wang, Y., and Wenk, C. (2006). “Fréchet distance for
696 curves, revisited.” *Lecture Notes in Computer Science (including subseries Lecture Notes in
697 Artificial Intelligence and Lecture Notes in Bioinformatics)*.
- 698 ASCE. (2016). *Minimum Design Loads for Buildings and Other Structures*. ASCE 7.
- 699 Benjamin, J. R., and Cornell, C. A. (2014). *Probability, Statistics, and Decision for Civil
700 Engineers*.
- 701 Bernardin, A., Hoyet, L., Mucherino, A., Gonçalves, D., and Multon, F. (2017). “Normalized
702 euclidean distance matrices for human motion retargeting.” *Proceedings - MIG 2017:
703 Motion in Games*.
- 704 Breiman, L. (2001). “2001 4_Method_Random_Forest.” *Machine Learning*.
- 705 Cakiroglu, C., Islam, K., Bekdaş, G., Isikdag, U., and Mangalathu, S. (2022). “Explainable
706 machine learning models for predicting the axial compression capacity of concrete filled
707 steel tubular columns.” *Construction and Building Materials*.
- 708 Degtyarev, V. V., and Tsavdaridis, K. D. (2022). “Buckling and ultimate load prediction models
709 for perforated steel beams using machine learning algorithms.” *Journal of Building
710 Engineering*.
- 711 Ellingwood, B. R. (1994). “Probability-based codified design: past accomplishments and future
712 challenges.” *Structural Safety*.
- 713 Emmert-Streib, F., Yli-Harja, O., and Dehmer, M. (2020). “Explainable artificial intelligence and
714 machine learning: A reality rooted perspective.” *Wiley Interdisciplinary Reviews: Data
715 Mining and Knowledge Discovery*.
- 716 Feldman, L. R., and Bartlett, F. M. (2005). “Bond strength variability in pullout specimens with
717 plain reinforcement.” *ACI Structural Journal*.
- 718 Frank, I., and Todeschini, R. (1994). *The data analysis handbook*.
- 719 Franssen, J. M., and Dotreppe, J. C. (2003). “Fire tests and calculation methods for circular
720 concrete columns.” *Fire Technology*.
- 721 Friedman, J. H. (2001). “Greedy function approximation: A gradient boosting machine.” *Annals
722 of Statistics*.
- 723 IBC. (2018). *International Building Code*.
- 724 Ke, G., Meng, Q., Finley, T., Wang, T., Chen, W., Ma, W., Ye, Q., and Liu, T. Y. (2017).
725 “LightGBM: A highly efficient gradient boosting decision tree.” *Advances in Neural
726 Information Processing Systems*.

Please cite this paper as:

Naser M.Z., (2024). Integrating Machine Learning Models to Building Codes and Standards: Establishing Equivalence through Engineering Intuition and Causal Logic. *ASCE Journal of Structural Engineering*. <https://doi.org/10.1061/JSENDH.STENG-12934>.

- 727 Kent, J. T. (1983). “Information gain and a general measure of correlation.” *Biometrika*.
- 728 Kodur, V. K. R. (1999). “Performance-based fire resistance design of concrete-filled steel
729 columns.” *Journal of Constructional Steel Research*, 51(1), 21–36.
- 730 Kodur, V., and MacKinnon, D. (2000). “Design of concrete-filled hollow structural steel
731 columns for fire endurance.” *Engineering Journal-American Institute of Steel Construction*,
732 37(1), 13–24.
- 733 Krueger, D., Caballero, E., Jacobsen, J.-H., Zhang, A., Binas, J., Zhang, D., Priol, R. Le, and
734 Courville, A. (2021). “Out-of-Distribution Generalization via Risk Extrapolation (REx).”
735 PMLR.
- 736 Kuchma, D. A., Wei, S., Sanders, D. H., Belarbi, A., and Novak, L. C. (2019). “Development of
737 the one-way shear design provisions of ACI 318-19 for reinforced concrete.” *ACI Structural*
738 *Journal*.
- 739 Law, T. (2021). “Beyond Minimum: Proposition for Building Surveyors to Exceed the Minimum
740 Standards of the Construction Code.” *Journal of Legal Affairs and Dispute Resolution in*
741 *Engineering and Construction*.
- 742 Lie, T. T. (1992). *Structural Fire Protection*. (T. T. Lie, ed.), American Society of Civil
743 Engineers, New York.
- 744 Lundberg, S. M., and Lee, S. I. (2017). “A unified approach to interpreting model predictions.”
745 *Advances in Neural Information Processing Systems*.
- 746 Marasco, S., Fiore, A., Greco, R., Cimellaro, G. P., and Marano, G. C. (2021). “Evolutionary
747 Polynomial Regression Algorithm Enhanced with a Robust Formulation: Application to
748 Shear Strength Prediction of RC Beams without Stirrups.” *Journal of Computing in Civil*
749 *Engineering*.
- 750 McNeely, D. J., and Stanley, D. L. (1963). “Tensile Strength of Concrete.” *ournal of the*
751 *American Concrete Institute*, 751–761.
- 752 Molnar, C. (2019). “Interpretable Machine Learning. A Guide for Making Black Box Models
753 Explainable.” *Book*.
- 754 Naser, M. (2023a). *Machine Learning for Civil and Environmental Engineers: A Practical*
755 *Approach to Data-Driven Analysis, Explainability, and Causality*. Wiley.
- 756 Naser, M. Z. (2021a). “Observational Analysis of Fire-Induced Spalling of Concrete through
757 Ensemble Machine Learning and Surrogate Modeling.” *Journal of Materials in Civil*
758 *Engineering*, American Society of Civil Engineers, 33(1), 04020428.
- 759 Naser, M. Z. (2021b). “Demystifying Ten Big Ideas and Rules Every Fire Scientist & Engineer
760 Should Know About Blackbox, Whitebox & Causal Artificial Intelligence.”
- 761 Naser, M. Z. (2023b). *Leveraging artificial intelligence in engineering, management, and safety*

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- 762 of infrastructure. (M. Naser, ed.), Taylor & Francis.
- 763 Naser, M. Z., Amir, ·, and Alavi, H. (2021). “Error Metrics and Performance Fitness Indicators
764 for Artificial Intelligence and Machine Learning in Engineering and Sciences.”
765 *Architecture, Structures and Construction 2021*, Springer, 1, 1–19.
- 766 Naser, M. Z., and Ross, B. (2022). “An opinion piece on the dos and don’ts of artificial
767 intelligence in civil engineering and charting a path from data-driven analysis to causal
768 knowledge discovery.” <https://doi.org/10.1080/10286608.2022.2049257>, Taylor & Francis.
- 769 NDS. (2018). *Technical Report No. 10 Calculating the Fire Resistance of Exposed Wood*
770 *Members*.
- 771 Ollgaard, J. G., Slutter, R. G., and Fisher, J. W. (1971). “Shear Strength of Stud Connectors in
772 Lightweight and Normal-Weight Concrete.” *AISC Engineering Journal*.
- 773 Paleyes, A., Urma, R. G., and Lawrence, N. D. (2022). “Challenges in Deploying Machine
774 Learning: A Survey of Case Studies.” *ACM Computing Surveys*, Association for Computing
775 Machinery, 55(6).
- 776 Raphael, J. M. (1984). “Tensile Strength of Concrete.” *Journal of the American Concrete*
777 *Institute*, 81, 158–165.
- 778 Reineck, K. H., Kuchma, D. A., Kim, K. S., and Marx, S. (2003). “Shear database for reinforced
779 concrete members without shear reinforcement.” *ACI Structural Journal*.
- 780 Ribarič, M., Šušteršič, L., and Stefan, J. (2008). “Empirical relationship as a stepping-stone to
781 theory.” *Arxiv*.
- 782 Ribeiro, M. T., Singh, S., and Guestrin, C. (2016). “‘Why should i trust you?’ Explaining the
783 predictions of any classifier.” *Proceedings of the ACM SIGKDD International Conference*
784 *on Knowledge Discovery and Data Mining*.
- 785 Riley, R. D., Snell, K. I. E., Ensor, J., Burke, D. L., Harrell, F. E., Moons, K. G. M., and Collins,
786 G. S. (2019). “Minimum sample size for developing a multivariable prediction model:
787 PART II - binary and time-to-event outcomes.” *Statistics in Medicine*.
- 788 Scikit. (n.d.). “1.4. Support Vector Machines — scikit-learn 0.24.1 documentation.”
789 <<https://scikit-learn.org/stable/modules/svm.html>> (Apr. 5, 2021).
- 790 Scikit. (2020). “sklearn.ensemble.GradientBoostingRegressor — scikit-learn 0.24.1
791 documentation.” <[https://scikit-](https://scikit-learn.org/stable/modules/generated/sklearn.ensemble.GradientBoostingRegressor.html)
792 [learn.org/stable/modules/generated/sklearn.ensemble.GradientBoostingRegressor.html](https://scikit-learn.org/stable/modules/generated/sklearn.ensemble.GradientBoostingRegressor.html)>
793 (Feb. 9, 2021).
- 794 Smeden, M. van, Moons, K. G., Groot, J. A. de, Collins, G. S., Altman, D. G., Eijkemans, M. J.,
795 and Reitsma, J. B. (2018). “Sample size for binary logistic prediction models: Beyond
796 events per variable criteria.” <https://doi.org/10.1177/0962280218784726>, SAGE
797 PublicationsSage UK: London, England, 28(8), 2455–2474.

Please cite this paper as:

Naser M.Z., (2024). Integrating Machine Learning Models to Building Codes and Standards: Establishing Equivalence through Engineering Intuition and Causal Logic. *ASCE Journal of Structural Engineering*. <https://doi.org/10.1061/JSENDH.STENG-12934>.

- 798 Smith, G. (1986). *Probability and statistics in civil engineering*. Collins, London.
- 799 Tapeh, A., and Naser, M. Z. (2022). “Artificial Intelligence, Machine Learning, and Deep
800 Learning in Structural Engineering: A Scientometrics Review of Trends and Best
801 Practices.” *Archives of Computational Methods in Engineering*.
- 802 Tarawneh, A., Momani, Y., and Alawadi, R. (2021). “Leveraging artificial intelligence for more
803 accurate and reliable predictions of anchors shear breakout capacity in thin concrete
804 members.” *Structures*.
- 805 Wade, C., Cowles, G., Potter, R., and Sanders, P. (1997). “Concrete Blade Columns in Fire wade
806 - Google Scholar.” *Concrete 97 Conference*, Adelaide, Australia.
- 807 Windapo, A., and Cattell, K. (2010). “A study of building contractors’ compliance with national
808 building regulations in Cape Town.” *COBRA 2010 - Construction, Building and Real Estate
809 Research Conference of the Royal Institution of Chartered Surveyors*.
- 810 XGBoost Python Package. (2020). “Python Package Introduction — xgboost 1.4.0-SNAPSHOT
811 documentation.” <[https://xgboost.readthedocs.io/en/latest/python/python_intro.html#early-
812 stopping](https://xgboost.readthedocs.io/en/latest/python/python_intro.html#early-stopping)> (Feb. 10, 2021).
- 813 Yahiaoui, A., Dorbani, S., and Yahiaoui, L. (2023). “Machine learning techniques to predict the
814 fundamental period of infilled reinforced concrete frame buildings.” *Structures*, Elsevier,
815 54, 918–927.
- 816 Yakubu, S. (2019). “Determinants of non-compliance with structural building code standards in
817 Nigeria.” *Proceedings of Institution of Civil Engineers: Management, Procurement and
818 Law*.
- 819